## Algebra 2

Name:
$1^{\text {st }}$ Semester Final Review \#3

1. Name the property of real numbers illustrated by each equation.
a) $2(3+\sqrt{5})=2 \cdot 3+2 \cdot \sqrt{5}$
b) $16+(-13)=-13+16$
c) $5(0.2 \cdot 7)=(5 \cdot 0.2) \cdot 7$
2. Solve the compound inequality. Graph the solution. $3 x>-6$ and $2 x<6$

3. Graph the equation. $4 x+3 y=12$

4. Write an equation for each line.
a) $m=-4$ and the $y$-intercept is 3 .
b) $m=-1$ and the $y$-intercept is 2 .
5. Find the slope and $y$-intercept of the line.

6. In the following problems, $y$ varies directly with $x$.
a) If $y=3$ when $x=-9$, find $x$ when $y=5$.
b) If $y=-14$ when $x=-7$, find $x$ when $y=22$.
c) If $y=5$ when $x=8$, find $x$ when $y=2$.
d) If $y=4$ when $x=14$, find $y$ when $x=5$
7. Find the slope and $y$-intercept of each line.
a) $3 x-4 y=12$
b) $y=-2$
c) $4 x-3 y=-6$
d) $f(x)=\frac{5}{4} x+7$
8. Find the slope of the line that passes through each pair of points.
a) $(-3,-2)$ and $(1,6)$
b) $(4,-1)$ and $(-2,-3)$

| 9. Determine whether $y$ varies directly with $x$. If so, find the constant of variation. <br> a) $y=\frac{4}{9} x$ <br> b) $y+4 x=0$ | 13. Solve by elimination. $\left\{\begin{array}{r} x+5 y=1 \\ 2 x+10 y=2 \end{array}\right.$ |
| :---: | :---: |
| c) $y=3 x \quad$ d) $y+2=x$ |  |
| 10. Write an absolute value equation or inequality to describe each graph. <br> a) <br> b) | 14. Solve the system of inequalities by graphing. $\begin{aligned} & y \geq x-3 \\ & y \leq \frac{-1}{2} x+2 \end{aligned}$  |
| 11. Without graphing, determine whether each system is consistent or inconsistent. <br> a) $\left\{\begin{array}{l}2 x+y=3 \\ y=-2 x-1\end{array}\right.$ <br> b) $\left\{\begin{array}{l}x+3 y=9 \\ 9 y+3 x=27\end{array}\right.$ | 15. Find the maximum or minimum values of the objective function. $\left\{\begin{array}{l} x \leq 4 \\ y \leq 3 \\ x \geq 0 \\ y \geq 0 \end{array} \text { maximum for } P=2 x+y\right.$  |
| 12. Solve by substitution. $\left\{\begin{array}{l} y=x+1 \\ 2 x+y=7 \end{array}\right.$ | 16. Solve by elimination. $\left\{\begin{aligned} x+y+z= & -4 \\ -x+2 y+3 z & =3 \\ x-4 y-2 z & =-15 \end{aligned}\right.$ |


| 17. Graph and list the vertex, tell if it is a max or min and list the axis of symmetry. $y=3(x-2)^{2}+1$  | 21. Factor and sketch the zeros of the function. $y=x^{3}-x^{2}-12 x$  |
| :---: | :---: |
| 18. Write each polynomial in standard form, classify it by degree and number of terms. <br> a) $3 c^{2}-4 c+9-4 c^{2}$ <br> b) $3 x^{2} y-3 x y-5 x^{2} y$ <br> c) $6 a^{2} b^{2} c^{1}$ <br> d) $5 x^{2}-5 x-x^{2}+x+4 x-6 x^{3}-1$ | 22. Factor each expression. <br> a) $16-64 p^{2}$ <br> b) $25 h^{3}-16 h$ <br> c) $4 k^{3}-24 k^{2}+36 k$ <br> d) $b^{2}-11 b+30$ |
| 19. Use $-\frac{b}{2 a}$ to determine the vertex. List the axis of symmetry and $y$-intercept for the quadratic equation and draw the graph. $y=x^{2}-2 x+3$  | 23. Factor each expression. <br> a) $8 x^{2}+13 x-6$ <br> b) $8 m^{3}-1$ <br> c) $6 x^{2}+28 x-10$ <br> d) $125+27 y^{3}$ |
| 20. Determine the standard form equation given the zeros. <br> a) $x=-3,1,0$ | 24. Use long division to divide. $x + 3 \longdiv { x ^ { 3 } + 2 x ^ { 2 } + 5 x + 1 2 }$ |

25. Use synthetic division to divide.

$$
\frac{4 n^{3}-6 n^{2}+2 n-7}{n-2}
$$

26. Evaluate by synthetic division.
. Find $P(-2)$ for $P(x)=x^{3}-4 x^{2}-x-6$
27. Expand using Pascal's triangle.

$$
(y-2)^{4}
$$

28. Categorize each number into one or more real number sets.
a) $\sqrt{7}$
b) -4
c) $\frac{12}{7}$
d) $3 \pi$
e) $-\frac{3}{4}$
29. Put the slope intercept form equation $y=-\frac{1}{5} x-2$ into standard form.
30. Graph each and list the vertex, tell if it is a max or min and list axis the of symmetry.

$$
y=-7(x+2)^{2}-1
$$


31. Solve each equation and graph the solution.
a) $|2 c-6|-9=5$

b) $|2 y-18|+4<10$

32. Solve each inequality. Graph the solution.
a) $-3 x-11 \geq 1$

b) $-3<-2 x+13<1$


